

# Learning Variable Mappings to Repair and Verify Programs

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CTU IN PRAGUE**

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- Thus, repairing an incorrect program based on a correct implementation is challenging.
- To compare both programs, program repair tools need to find a relation between these programs' variables.

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Function that finds and returns the maximum number among  $n_1$ ,  $n_2$  and  $n_3$ .

```
1  int max(int n1, int n2, int n3)
2  {
3      int m = n1 > n2 ? n1 : n2;
4      return n3 > m ? n3 : m;
5  }
```

Function that finds and returns the maximum number among  $x$ ,  $y$  and  $z$ .

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Besides *program repair* [Ahmed et al., 2022], the task of mapping variables between programs is also important for:

- *program analysis*;
- *program equivalence*;
- *program verification*;
- *program clustering*;
- *clone detection*;
- *plagiarism detection*.



# Goal

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- Create a graph program representation that takes advantage of the structural information of the *abstract syntax trees (ASTs)* of programs;

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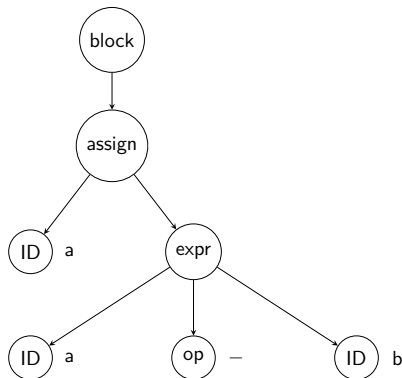
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- Create a graph program representation that takes advantage of the structural information of the *abstract syntax trees (ASTs)* of programs;
- Use our program representation to learn how to map the set of variables between a correct program and a faulty one using *graph neural networks (GNNs)*.

# Program Representation

An expression that uses int variables a and b, previously declared in the program.

```
1  {  
2    // a and b are ints  
3    a = a - b;  
4  }
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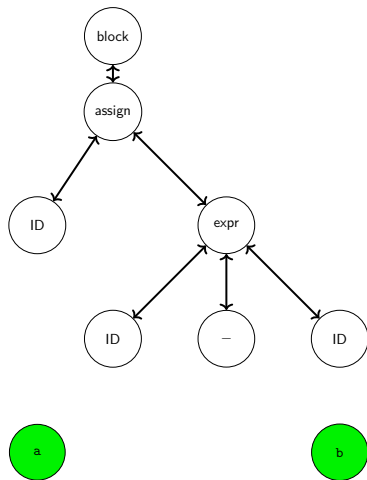


(a) Part of the AST representation.

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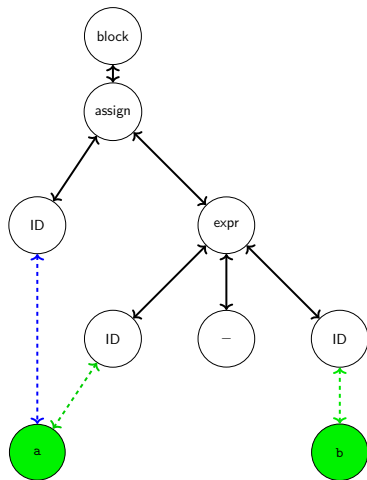


(b) Our program representation.

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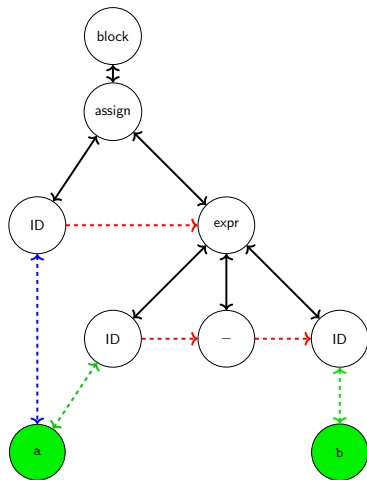


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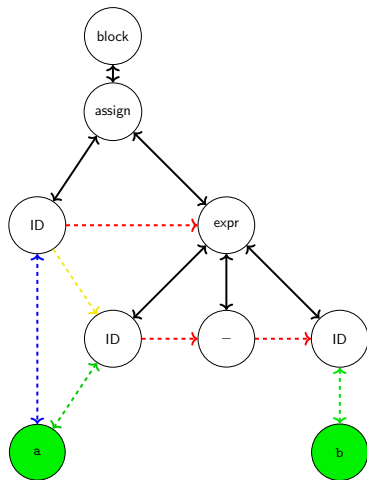


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- We perform *message passing* between the nodes of our representations, so that information can be passed between the local constituents;
- After several message passing rounds, we obtain numerical vectors corresponding to each variable node in the two programs;
- We compute scalar products between each possible combination of variable nodes in the two programs, followed by a softmax function.

# C-Pack-IPAs: Dataset of Introductory Programming Assignments (IPAs)

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**Table:** Description of C-PACK-IPAs [Orvalho et al., 2022].

<b>Academic Year</b>	<b>#IPAs</b>	<b>#Correct Submissions</b>	<b>#Incorrect Submissions</b>
<b>1<sup>st</sup> Year</b>	10	238	107
<b>2<sup>nd</sup> Year</b>	10	78	60

# Data Augmentation

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- Since we need to know the real variable mappings between programs to evaluate our representation, we used MULTIPAS [Orvalho et al., 2022] to generate a dataset of pairs of correct/incorrect programs.

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- Since we need to know the real variable mappings between programs to evaluate our representation, we used MULTIPAS [Orvalho et al., 2022] to generate a dataset of pairs of correct/incorrect programs.
- The second reason to use MULTIPAS was that our dataset, C-PACK-IPAS, is too small, i.e., contains only a few hundred submissions.

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The main goal of MULTIPAS is to augment IPAS benchmarks with:

- more semantically correct implementations (**program mutations**);
- new semantically incorrect programs (**program mutilations/bugs**);
- **variable mappings** between the original program and the mutated and/or mutilated program;
- information about the **types and the number of bugs** present in each generated incorrect program.

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- *Comparison Expression Mirroring;*
- *If-else-statements Swapping;*
- *Increment/Decrement Operators Mirroring;*
- *Variable Declarations Reordering;*
- *For-2-While Translation;*
- *Variable Addition.*

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  - variable misuse (VM);
  - missing expression (ME).



# Data Augmentation

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Original program.

```
1  int main(){
2      int n;
3      int i, s;
4      scanf("%d", &n);
5      s=0;
6      for(i=1; i<=n; i++){
7          s = s+i;
8          printf("%d\n",s);
9      }
10
11     printf("%d\n",s);
12     return 0;
13 }
```

Incorrect program.

```
1  int main(){
2      int n, s, i, y;
3      scanf("%d", &n);
4      s=0;
5      i = 1;
6      while(n>=i){
7
8          printf("%d\n",s);
9          ++i;
10     }
11     printf("%d\n",s);
12     return 0;
13 }
```

# C-Pack-IPAs: Augmented Dataset

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**Table:** The description of the training, validation, and evaluation sets based on C-PACK-IPAs.

	<b>Buggy Programs</b>			
	WCO Bug	VM Bug	ME Bug	All Bugs
Training set (1 <sup>st</sup> Year)	3372	5170	2908	11450
Validation set (1 <sup>st</sup> Year)	1457	1457	1023	3937
Evaluation set (2 <sup>nd</sup> Year)	1078	1936	1152	4166

# Use Cases: Program Repair

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- We use variable mappings to repair an incorrect program using a correct implementation for the same IPA without considering the programs' structures.
- We claim that variable mappings are informative enough to repair these three realistic types of bugs.

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- Given a buggy program, we search for and try to repair all three types of bugs;

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- Given a buggy program, we search for and try to repair all three types of bugs;
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- Then, by comparing the expressions of both programs, we try to fix the incorrect one by replacing the expressions that do not appear in the correct program, with the correct program's expressions;

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General idea:

- Given a buggy program, we search for and try to repair all three types of bugs;
- First, we rename all the variables in the incorrect program based on the variable mapping;
- Then, by comparing the expressions of both programs, we try to fix the incorrect one by replacing the expressions that do not appear in the correct program, with the correct program's expressions;
- Whenever we find a possible fix, we check if the program is correct using the test suite.



# Results

# Training

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**Table:** Validation mappings fully correct after 20 training epochs.

	<b>Buggy Programs</b>			
	WCO Bug	VM Bug	ME Bug	All Bugs
Accuracy	93.7%	95.8%	93.4%	96.49%

# Evaluation

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**Table:** The number of correct variable mappings generated by our GNN on the evaluation dataset and the average overlap coefficients between the real mappings and our GNN's variable mappings.

Evaluation Metric	Buggy Programs			
	WCO Bug	VM Bug	ME Bug	All Bugs
# Correct Mappings	87.38%	81.87%	79.95%	82.77%
Avg Overlap Coefficient	96.99%	94.28%	94.51%	95.05%

# Ablation Study

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**Table:** Percentage of variable mappings fully correct on the validation set for different sets of edges used. Each type of edge is represented by an index using the mapping: {0: AST; 1: sibling; 2: write; 3: read; 4: chronological}.

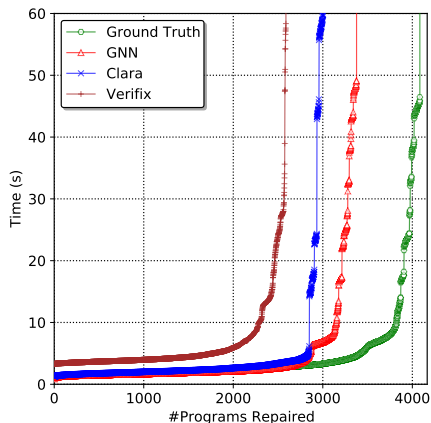
Edges Used	All	(1,2,3,4)	(0,2,3,4)	(0,1,3,4)	(0,1,2,4)	(0,1,2,3)	(0,1)
Accuracy	<b>96.49%</b>	52.53%	73.76%	95.45%	94.87%	96.06%	94.74%

# Repairing Programs

**Table:** The number of programs repaired by each different repair technique: VERIFIX, CLARA, and our repair approach based on our GNN's variable mappings. The last row shows the results of repairing the programs using the real variable mappings (ground truth).

Repair Method	Buggy Programs				Not Succeeded	
	WCO Bug	VM Bug	ME Bug	All Bugs	% Failed	% Timeouts (60s)
Verifix	555 (51.48%)	1292 (66.74%)	741 (64.32%)	2588 (62.12%)	1471 (35.31%)	107 (2.57%)
Clara	722 (66.98%)	1517 (78.36%)	764 (66.32%)	3003 (72.08%)	1153 (27.68%)	<b>10 (0.24%)</b>
GNN	<b>942 (87.38%)</b>	<b>1537 (79.39%)</b>	<b>898 (77.95%)</b>	<b>3377 (81.06%)</b>	<b>711 (17.07%)</b>	78 (1.87%)
Ground Truth	1078 (100.0%)	1877 (96.95%)	1129 (98.0%)	4084 (98.03%)	0 (0.0%)	82 (1.97%)

# Repairing Programs



**Figure:** Cactus plot - The time spent by each method repairing each program of the evaluation dataset, using a timeout of 60 seconds.

# Use-case: Program Verification

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- We can also use the variable mappings to map assertions between different programs.

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- We can also use the variable mappings to map assertions between different programs.
- This way, we can automatically verify students' submissions, using CBMC [Clarke et al., 2004], based on similar previously submitted correct implementations for the same programming exercise.



# Example: Program Verification

Variable Mapping:  $\{n : 1; i : j\}$ .

A semantically correct student's implementation.

```
1  int main(){
2      int n, i;
3      scanf("%d", &n);
4      for(i = 1; i <= n; i++){
5          assert(1 <= i && i <= n);
6          printf("%d\n", i);
7      }
8      return 0;
9  }
```

A semantically incorrect student's implementation since the variable  $j$  in the main function is not initialized.

```
1  void loop(int j, int l){
2      while (l >= j){
3          assert(1 <= j && j <= l);
4          printf("%d\n", j);
5          ++j;
6      }
7  }
8  int main(){
9      int j, l;
10     scanf("%d", &l);
11     loop(j, l);
12     return 0;
13 }
```

**Obrigado!**  
**Děkuju!**  
**Thank you!**

# References

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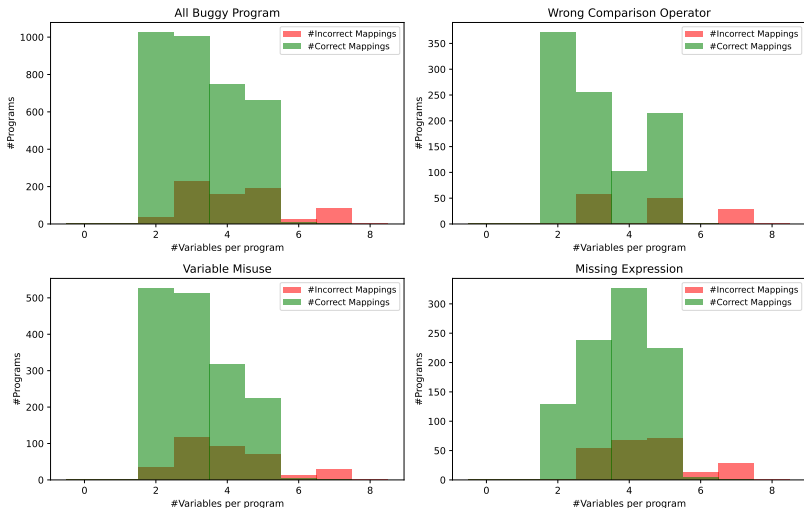
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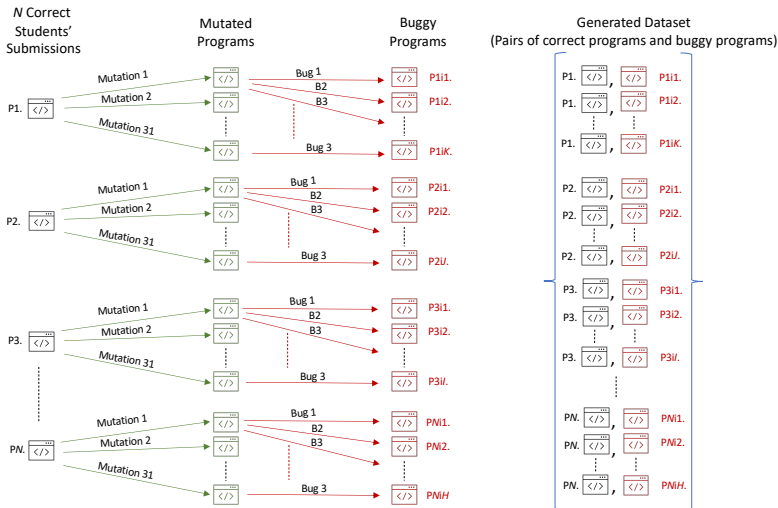
# Appendix

# #Correct/Incorrect Mappings vs #Variables

GNN Model trained on All Buggy Programs



# Dataset Generation using MultiIPAs



# Overlap coefficient

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The overlap or Szymkiewicz–Simpson coefficient measures the overlap between two sets (e.g. mappings). This metric can be calculated by dividing the size of the intersection of two sets by the size of the smaller set, as follows:

$$\text{overlap}(A, B) = \frac{|A \cap B|}{\min(|A|, |B|)} \quad (1)$$

An overlap of 100% means that both sets are equal or one of them is a subset of the other. The opposite, 0% overlap, means there is no intersection between both sets.